

# A non-admitted role of central banks: Debt-dependent quantitative monetary policies

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  - fiscal policy instruments react to public debt
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  - typically, this policy mix ensures stability and determinacy.

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- During the same period fiscal policies have been set exogenously to support the economy without reacting to debt imbalances.
- It seems that the politically unpleasant task of debt sustainability has fallen on Central Banks.

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- We explore the possibility that quantitative monetary policies can substitute tax-spending debt stabilization policies when it comes to stability and determinacy.

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- We explore the possibility that quantitative monetary policies can substitute tax-spending debt stabilization policies when it comes to stability and determinacy.
- We do so in the context of a rather standard New Keynesian general equilibrium model solved using common parameter values and data from the EZ.

- Step A: We shock the initial steady state by assuming an adverse supply shock (to mimic an economic disaster) and, at the same time, an increase in government transfers (to mimic the usual fiscal stimulus that counters economic disasters) - see Hall and Sargent (2021).



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  - A policy instrument needs to react to outstanding public debt to restore stability.
- Step B: We experiment with different debt-contingent policy instruments, both fiscal and (quantitative) monetary.

- Leeper (1991)
- Reis (2016, 2017)
- Coenen et al (2018, 2020)
- Masuch et al (2018)
- Sims and Wu (2020)
- Bassetto and Sargent (2020)
- Hall and Sargent (2021)

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  - which means that market segmentation and costly financial intermediation give rise to asset pricing wedges and imperfect substitutability that break Wallace's (1981) neutrality proposition and give a real role to quantitative monetary policies (Walsh, 2017, chapter 11, for a review)

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- **budget constraint.** ▶ GBC

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- liabilities: banknotes and reserves (TARGET2 balances are cancelled out at ES level)
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- In simple words, the issuance of liabilities is used to finance, via loans to private banks, loans to private companies and national governments, via government bonds purchases in the secondary market.



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  - The end-of-period government bonds follow residually to close the Treasury's budget constraint.

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- The lack of “fiscal backing” in the EZ implies that the CB's dividends to Treasury,  $n_t$ , is an exogenous policy instrument (see Del Negro and Sims (2015), Hall and Reis (2017)). Also, the lack of “fiscal support” in the EZ, implies the non-negativity constraint:  $n_t \geq 0$ .

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- To the extent that currency held by the non-bank public and reserves, as well as central bank loans held by private banks are demand determined, the central bank's budget constraint can provide an extra equation to determine the inflation rate or the price level.

- We adopt a rule-like approach to policy where the exogenous policy instruments, in addition to a conventional exogenous  $AR(1)$  component, can also react to debt imbalances.
- The rules of the tax-spending instruments are:

$$s_t = \rho^s s_{t-1} + (1 - \rho^s) s - \gamma^s \left( \frac{b_t}{y_t} - \frac{b}{y} \right)$$

$$\tau_t = \rho^\tau \tau_t + (1 - \rho^\tau) \tau_{t-1} + \gamma^\tau \left( \frac{b_t}{y_t} - \frac{b}{y} \right)$$

# Monetary policy rules

- The policy rates,  $i_t^z$  and  $i_t^r$ , follow Taylor type rules of the form:

$$\log(1 + i_t) = (1 - \rho) \log(1 + i) + \rho \log(1 + i_{t-1}) + \gamma^\pi \log(\pi_t / \pi)$$

- The central bank purchases in the secondary market the fraction  $(1 - \Lambda_t)$  of outstanding government bonds, at a constant price  $\Phi_t$ , where  $(1 - \Lambda_t)$  satisfies:

$$\Phi_t (1 - \Lambda_t) \frac{p_{t-1}}{p_t} b_{t-1} = B_t y_t$$

and

$$B_t = \rho^B B_{t-1} + \gamma^B \left( \frac{b_t}{y_t} - \frac{b}{y} \right)$$

## Monetary policy rules (cont'ed)

- The CB pays out to Treasury its non-negative net income every period (see e.g. Reis, 2016, 2017):

$$n_t = \left( m_{h,t} - \frac{p_{t-1}}{p_t} m_{t-1} \right) + i_t^z \frac{p_{t-1}}{p_t} z_{p,t-1} + \\ + i_t^b (1 - \Lambda_t) \frac{p_{t-1}}{p_t} b_{t-1} - i_t^r \frac{p_{t-1}}{p_t} m_{p,t-1}$$

and

$$n_t \geq 0$$

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- **Deterministic (perfect foresight equilibrium); non-linear dynamics; use dynare toolbox.**

# The impact of economic policy

- To quantify the impact of the different policies on the economy, we plot of the Impulse Response Functions (IRFs) of the main macroeconomic variables and calculate a “multiplier” (close to Uhlig’s, 2010, multipliers),  $\varphi_t$ , which is given by:

$$\varphi_t = \sum_{s=0}^t \frac{y_s - y}{(1 + i_b)^s}$$

- We have experimented with other criteria, like the discounted lifetime utility in terms of consumption equivalents (see e.g. Lucas (1990)) and the the welafre losses (see e.g. Schmitt-Grohé and Uribe (2007)), and the results are quantitatively close.

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# Policy scenaria

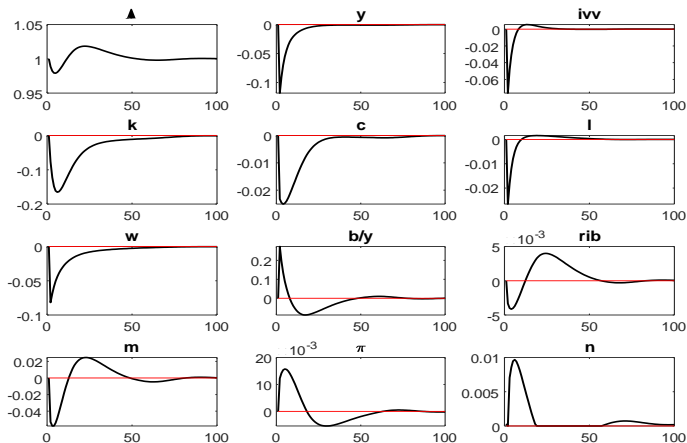
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  - **"Fiscal dominance"**: quantitative monetary policy substitutes fiscal policy when it comes to debt stability and determinancy.

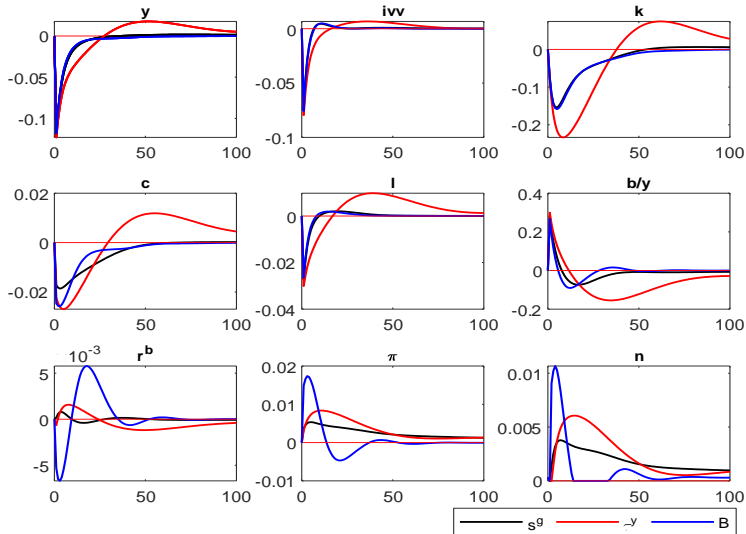
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    - we switch off fiscal reaction to debt and allow CB’s government bonds’ purchases in the secondary market to react to debt imbalances.
- For all policy rules considered we set the persistence parameter  $\rho = 0.8$ , while we set the feedback parameter,  $\gamma$ , to the lowest possible value that ensures dynamic stability.

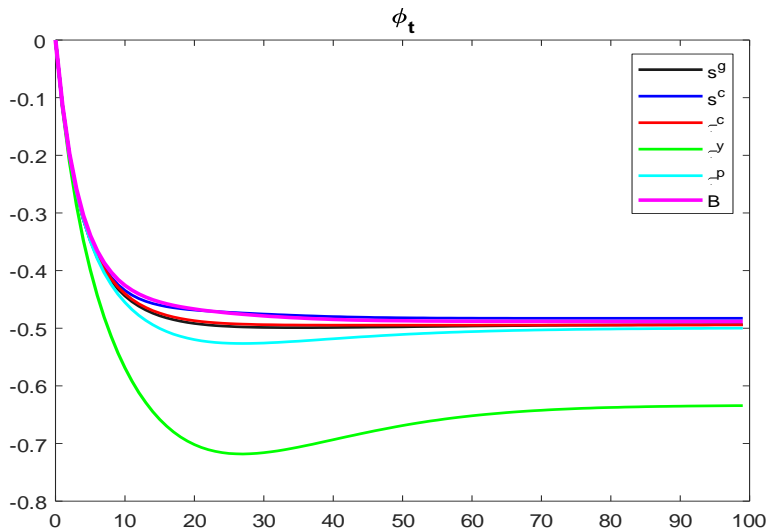
# CB's government bond purchases



# Fiscal and monetary policy instruments



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- Debt-dependent quantitative monetary policy can ensure stability and determinacy at a smaller real cost than tax debt-dependent policies.
- But this:
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  - makes debt-to-GDP ratio more volatile: the ratio de-escalates quickly in the short-run but increases again in the medium-run when the CB sells government bonds
  - comes at a cost of higher inflation.

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• Thank you for your attention

## Budget constraint:

$$\begin{aligned} & (1 + \tau_t^c)c_{h,t} + j_{h,t} + m_{h,t} = \\ & = (1 - \tau_t^y)w_t l_{h,t} + (1 + i_t^d) \frac{p_{t-1}}{p_t} j_{h,t-1} + \frac{p_{t-1}}{p_t} m_{h,t-1} + \pi_{h,t} + g_t^t \end{aligned}$$

## Cash-in-advance constraint:

$$m_{h,t} \geq (1 + \tau_t^c)c_{h,t}$$

▶ households



## Standard Dixit-Stiglitz technology:

$$y_{f,t} = \left[ \sum_{i=1}^N \frac{1}{N} (y_{i,t})^\theta \right]^{\frac{1}{\theta}}$$

## Real profits:

$$\pi_{f,t} = y_{f,t} - \sum_{i=1}^N \frac{1}{N} \frac{p_{i,t}}{p_t} y_{i,t}$$

▶ private firms

## Net profit:

$$\pi_{i,t} = (1 - \tau_t^\pi) \left[ \frac{p_{i,t}}{p_t} y_{i,t} - w_t l_{i,t} \right] - x_{i,t} - \frac{\zeta^p}{2} \left( \frac{p_{i,t}}{p_{i,t-1}} - 1 \right)^2 \bar{y}_{i,t}^h + \left( L_{i,t}^h - [1 + i_t^l (1 - \tau_t^\pi)] \frac{p_{t-1}}{p_t} L_{i,t-1}^h \right)$$

## Production function:

$$y_{i,t} = A (k_{t-1}^g)^\sigma (k_{i,t-1}^\alpha l_{i,t}^{1-\alpha})^{1-\sigma}$$

**The law of motion of the firm's capital stock:**

$$k_{i,t} = x_{i,t} + (1 - \delta) k_{i,t-1}$$

**Borrowing constraint:**

$$L_{i,t} \geq \eta w_t l_{i,t}$$

**Demand for product:**

$$p_{i,t} = p_t \left( \frac{y_{i,t}}{y_{f,t}} \right)^{\theta-1}$$

▶ private firms

# Private banks

The budget constraint of each bank that connects changes in its assets and liabilities is:

$$\begin{aligned}\pi_{p,t} = & (1 - \tau_t^\pi) \left[ (1 + i_t^l) \frac{p_{t-1}}{p_t} L_{p,t-1} + (1 + i_t^r) \frac{p_{t-1}}{p_t} m_{p,t-1} + (1 + i_t^b) \frac{p_{t-1}}{p_t} \Lambda_t b_{p,t-1} \right. \\ & \left. + \Phi_t \frac{p_{t-1}}{p_t} (1 - \Lambda_t) b_{p,t-1} - (1 + i_t^d) \frac{p_{t-1}}{p_t} j_{p,t-1} - (1 + i_t^z) \frac{p_{t-1}}{p_t} z_{p,t-1} - \Xi_t \right] - \\ & - L_{p,t} - b_{p,t} - m_{p,t} + j_{p,t} + z_{p,t}\end{aligned}$$

where

$$\begin{aligned}\Xi_t = & \frac{\zeta^l}{2} (L_{p,t-1})^2 + \frac{\zeta^b}{2} (\Lambda_t b_{p,t-1})^2 + \\ & + \frac{\zeta^m}{2} (m_{p,t-1} + \Phi_t (1 - \Lambda_t) b_{p,t-1})^2 + \frac{\zeta^z}{2} (z_{p,t-1})^2\end{aligned}$$

# The Government budget constraint

The flow budget constraint of the government written in per capita and real terms is:

$$g_t^c + g_t^g + g_t^t + (1 + i_t^b) \frac{p_{t-1}}{p_t} b_{t-1} = b_t + \frac{T_t}{N} + n_t$$

Total tax revenues in real terms are defined as:

$$\begin{aligned} \frac{T_t}{N} \equiv & \tau_t^c c_{h,t} + \tau_t^y w_t l_{h,t} + \tau_t^\pi (y_{i,t} - w_t l_{i,t}) + \\ & + \tau_t^\pi \left[ (1 + i_t^l) \frac{p_{t-1}}{p_t} L_{p,t-1} + (1 + i_t^r) \frac{p_{t-1}}{p_t} m_{p,t-1} + \right. \\ & + (1 + i_t^b) \frac{p_{t-1}}{p_t} \Lambda_t b_{p,t-1} + \Phi_t \frac{p_{t-1}}{p_t} (1 - \Lambda_t) b_{p,t-1} - \\ & \left. - (1 + i_t^d) \frac{p_{t-1}}{p_t} j_{p,t-1} - (1 + i_t^z) \frac{p_{t-1}}{p_t} z_{p,t-1} - \frac{p_t^h}{p_t} \Xi_t \right] \end{aligned}$$

# The central bank

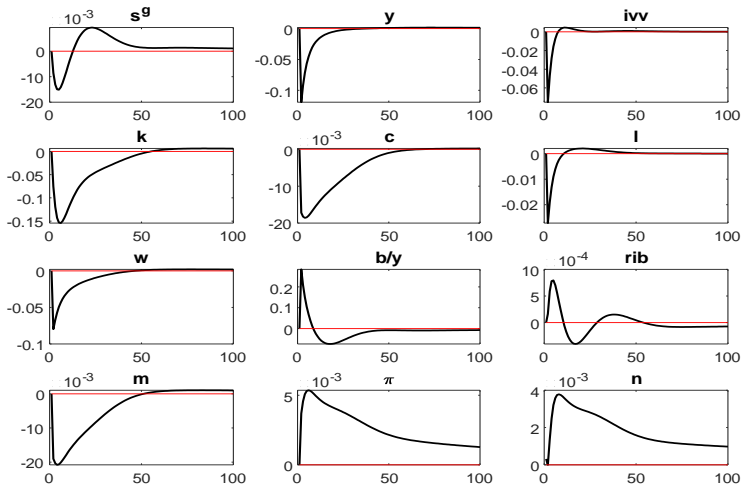
The budget constraint of the CB linking changes in assets and liabilities is (written in real and per capita terms):

$$\Phi_t(1 - \Lambda_t) \frac{p_{t-1}}{p_t} b_{t-1} + z_{p,t} + i_t^r \frac{p_{t-1}}{p_t} m_{p,t-1} + n_t \equiv$$

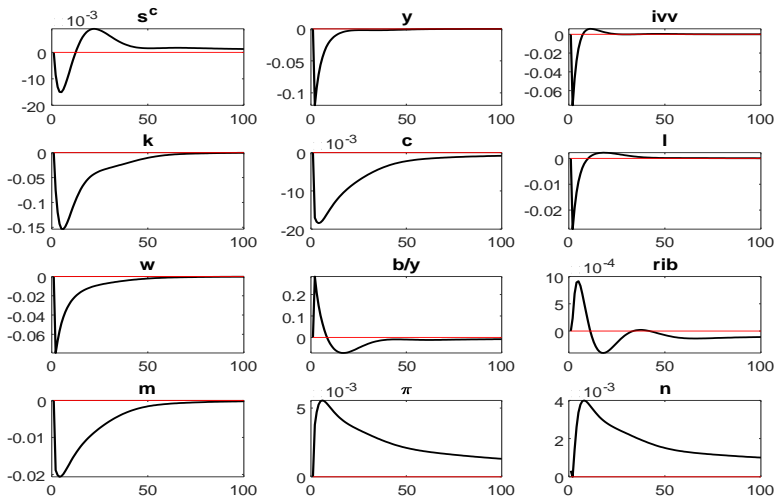
$$\equiv (1 - \Lambda_t)(1 + i_t^b) \frac{p_{t-1}}{p_t} b_{t-1} + (1 + i_t^z) \frac{p_{t-1}}{p_t} z_{p,t-1} + m_t - \frac{p_{t-1}}{p_t} m_{t-1}$$

▶ central bank

# Government investment

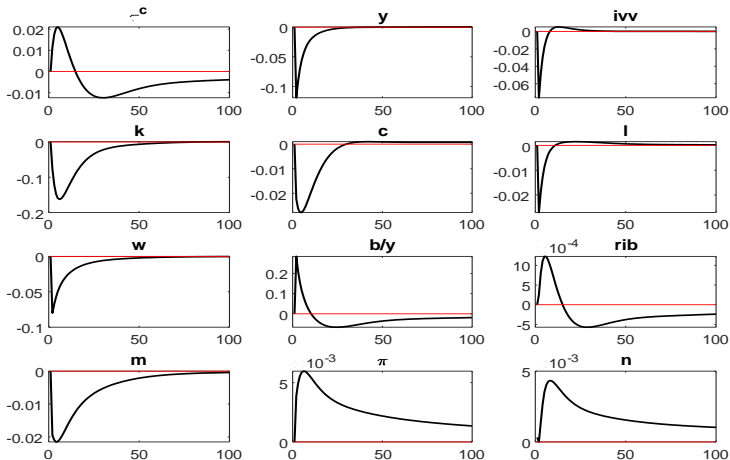


# Government consumption

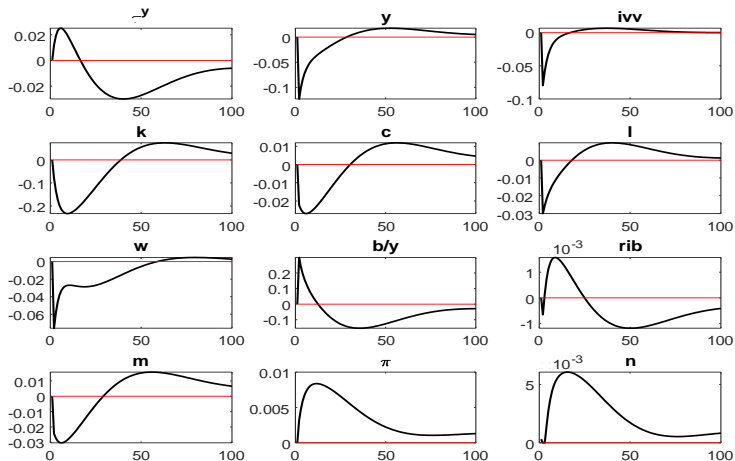




# Consumption tax rate



# Income tax rate



# Profit tax rate

